DATA ANALYTICS REFERENCE DOCUMENT					
Document Title:	Document Title				
Document No.:	1594121056				
Author(s):	Gerhard van der Linde				
Contributor(s):					

REVISION HISTORY

Revisior	Details of Modification(s)	Reason for modification	Date	Ву
0	Draft release	Document description here	2020/07/07 11:24	Gerhard van der Linde

Top 20 Dynamic programming Questions

- 1. Longest Common Subsequence
- 2. Longest Increasing Subsequence
- 3. Edit Distance
- 4. Minimum Partition
- 5. Ways to Cover a Distance
- 6. Longest Path In Matrix
- 7. Subset Sum Problem
- 8. Optimal Strategy for a Game
- 9. 0-1 Knapsack Problem
- 10. Boolean Parenthesization Problem
- 11. Shortest Common Supersequence
- 12. Matrix Chain Multiplication
- 13. Partition problem
- 14. Rod Cutting
- 15. Coin change problem
- 16. Word Break Problem
- 17. Maximal Product when Cutting Rope
- 18. Dice Throw Problem
- 19. Box Stacking
- 20. Egg Dropping Puzzle

Longest Common Subsequence

```
# Longest Common Subsequence
```

```
# LCS Problem Statement: Given two sequences, find the length of
```

```
# longest subsequence present in both of them. A subsequence is a
```

```
# sequence that appears in the same relative order, but not
```

```
# "aeg", '"acefg", .. etc are subsequences of "abcdefg".
```

```
s=('ABCDGH')
t=('AEDFHR')
```

```
step=2
def lcs(X, Y, m, n):
 # naive
    if m == 0 or n == 0:
       return 0;
    elif X[m-1] == Y[n-1]:
      return 1 + lcs(X, Y, m-1, n-1);
    else:
      return max(lcs(X, Y, m, n-1), lcs(X, Y, m-1, n));
def lcs_d(X , Y):
   # find the length of the strings
    m = len(X)
    n = len(Y)
    # declaring the array for storing the dp values
    L = [[None]*(n+1) for i in range(m+1)]
    '''Following steps build L[m+1][n+1] in bottom up fashion
    Note: L[i][j] contains length of LCS of X[0..i-1]
    and Y[0..j-1]'''
    for i in range(m+1):
        for j in range(n+1):
            if i == 0 or j == 0:
                L[i][j] = 0
            elif X[i-1] == Y[j-1]:
                L[i][j] = L[i-1][j-1]+1
            else:
                L[i][j] = max(L[i-1][j] , L[i][j-1])
    # L[m][n] contains the length of LCS of X[0..n-1] & Y[0..m-1]
    return L[m][n]
#end of function lcs
print(lcs(s,t,len(s),len(t)))
```

```
print(lcs_d(s,t))
```

Longest Increasing Subsequence

TestList: [22, 33, 55, 42, 63, 31, 44, 82, 84, 96] Result: 7 --> [22, 33, 55, 63, 82, 84, 96]

Arr[]	22	33	55	42	63	31	44	82	84	96
LIS	1	2	3	-	4	-	-	5	6	7

Longest Increasing Subsequence
import numpy as np

```
def lis():
    #n=[10, 22, 9, 33, 21, 50, 41, 60, 80]
    n=list(np.random.randint(1,100,10))
    #print(n)
    test={} # create an empty library for the tests
    for i in range(len(n)):
```

```
#print()
    seq=[]
    seq.append(n[i])
    big=n[i]
    for j in range(i,len(n)):
     #print(i,j)
     if n[j]>big:
        seq.append(n[j])
        big=n[j]
    #print(seq)
    test[i]=seq
  return test
# find the longest list
for i in range(1000):
  test=lis()
  l=test[list(map(lambda x: len(x),test.values())).index(max(list(map(lambda x:
len(x),test.values())))]
  if len(l) > 5:
    print(len(l),'-->',l)
```

Edit Distance

Given two strings str1 and str2 using the lister operations that can performed on str1. Find minimum number of edits (operations) required to convert 'str1' into 'str2'.

- 1. Insert
- 2. Remove
- 3. Replace

All of the above operations are of equal cost.

```
Examples:
    Input: strl = "geek", str2 = "gesek"
    utput: 1
    Comment: We can convert strl into str2 by inserting a 's'.
```

The *Levenshtein* distance is a string metric for measuring the difference between two sequences. Informally, the Levenshtein distance between two words is the minimum number of single-character edits (insertions, deletions or substitutions) required to change one word into the other. It is named after the Soviet mathematician Vladimir Levenshtein, who considered this distance in 1965.

```
\begin{aligned} & \ (i,j) = \ (i,j) =
```

Levenshtein distance may also be referred to as edit distance, although that term may also denote a larger family of distance metrics known collectively as edit distance. It is closely related to pairwise string alignments.

	X										
У			g	е	е	k					
		0	1	2	3	4					
	g	1	0	1	2	3					
	е	2	1	0	1	2					
	S	3	2	1	1	2					
	е	4	3	2	1	2					
	k	5	4	3	2	1					

So for every row and column there is only two cases:

- The pair match
- The pair do not match

у	x						
			g	е	е	k	
		0	1	2	3	4	
	g	1	0	1	2	3	
	е	2	1	0	1	2	
	s	3	2	1	1	2	
	е	4	3	2	1	2	
	k	5	4	3	2	1	

If the pair match copy the diagonal value across

у	Х								
		g e e k							
		0	1	2	3	4			
	g	1	0	1	2	3			
	е	2	1	0	1	2			
	s	3	2	1	1	2			
	e	4	3	2	1	2			
	k	5	4	3	2	1			

If the pair do not match, take the smallest of the three values highlighted and ${\bf add} \ {\bf 1}.$

2024/05/02 13:18

5/10

Implementation in Python using Matrixes

```
import numpy as np
def getEditLen(inw, outw, verbose=False):
  return the Levenstein distance between two word using the Levenstein formula implemented in
python
  using a numpy array.
  input: Two strings to compare, example 'geek' and 'gesek'
  output: The number of edits required using insert, delete or replace to turn the input word
          into the output word.
  opetions: verbose=False|True, default is False
  Example: Calculate the distance between 'geek' and 'gesek'
  Compare the entire matrix row by row, starting with null cases answering the fundamental
question for
  line g, how many edits is needed to turn g into g, g into ge, g into gee and g into geek and
the answers
  would be 0,1,2,3 and so on.
  The second way to answer the question for every cell is, are the letters different or are the
matched.
  If matched copy the value to the top left cell diagonally down. If the letters are different
determine
  the lowest value of the three cell, left, top or diagonal left plus one to the cell. Keep on
doing this
  till all the cells are filled.
  | | |g|e|e|k|
  | |0|1|2|3|4|
  |g|1|0|1|2|3|
  |e|2|1|0|1|2|
  |s|3|2|1|1|2|
  |e|4|3|2|1|2|
  |k|5|4|3|2|1|
  The final answer to the problem is now in the bottom right cell and can be returned by the
function call.
  1.1.1
  # create an empty array for storing results
  #get the arary dimensions
  liw=len(inw)
  low=len(outw)
  #create an empty array
  ar=np.zeros((liw+1,low+1), dtype=np.int)
  #initialise the null array rows and columns
  for i in range(low+1): ar[0][i]=i
  for i in range(liw+1): ar[i][0]=i
  if verbose: print(ar)
  for i in range(len(inw)):
    row=i+1
    for o in range(len(outw)):
     col=o+1
      if verbose: print('{}[{}] == {}[{}] --> '.format(inw[i],i,outw[o],o), end='')
      if inw[i] == outw[o]: # if the letters match do this
       if verbose: print('True',' -->', ar[row-1][col-1])
        ar[row][col]=ar[row-1][col-1] # copy the value diagonally down, i.e one row up, one
```

HDip Data Analytics - http://hdip-data-analytics.com/

Last update: 2020/07/07 programming:dynamic_programmig_questions http://hdip-data-analytics.com/programming/dynamic_programmig_questions?rev=1594121283 11:28

```
columen left
    else: # if the letters do not match, do this part
    if verbose: print('False','-->',min(ar[row-1][col],ar[row][col-1],ar[row-1][col-1])+1)
    # set te smallest value of the three columns, left, above or between plus one.
    ar[row][col]=min(ar[row-1][col],ar[row][col-1],ar[row-1][col-1])+1
    if verbose: print(ar)
    return ar[-1][-1] # return the bottom right value as the final answer.

if __name__ == '__main__':
    wlen=getEditLen('geek', 'gesek', verbose=False)
    print('The Levenstein length is: {}'.format(wlen))
```

References

https://docs.python.org/3/library/stdtypes.html?highlight=center#text-sequence-type-str

Minimum Partition

The objective of this exercise is to create two lists from once list of values and divide them in such a way that the difference of the sum of each list is the smallest possible solution for the numbers available.

With a short list of numbers a more thorough comparison is needed and all possible permutations must be tested to get the minimum difference. As the list size is increased a faster approach is needed for time efficiency and also the need to compare all permutation is no longer needed since multiple solutions becomes available.

A short solution for longer lists is to sort tow lists is ascending and descending order and subtract the one for the other and find the nearest solution to the sum of differences and swop the values around in the list to get the minimum error.

Testing this over a ranges of lengths works without fail.

The code below show the two tiered approach for this solution and includes time efficiencies generating the solutions.

```
import numpy as np
from time import time
def split(l):
  This function sorts the list from small to big and devide into two
  lists of equal length.
  input: a list of variables
  output: two lists of variables of very similar sums
  1.1.1
  l.sort()
  a,b=[],[]
  for i in range(len(l)):
    if i%2==0:
      a.append(l[i])
    else:
      b.append(l[i])
  return a.b
def bestdiff(a,b,verbose=False):
  This function takes two lists of integer values and balances the list
  to be a close as possible to equal sums or in other words to have the
```

```
2024/05/02 13:18
```

7/10

```
minimum difference in sums.
 Inputs: Two lists in integeres and verbose processing or not, default off
  Outputs: Two balanced lists of integeres and a flag for the fast or
  slow method. The slow method is more accurate and needed for very short
  lists while the fast method is best suited for longer lists. Lists over
  1000 values in length takes very long to comlete using the slow method
  and does not yiled better results.
  1.1.1
  tlen=len(a)+len(b) # total length of both lists
  if verbose: print('Lengt of testarray: {}'.format(tlen))
  t = (sum(a) - sum(b))  # caalculate the delta between the lists entered
  if verbose: print(t/2) # show the half of the delta
  if t < 0: # if the delta is smaer than zero swop lists a and b
   b_{a=a,b}
  d=[int((i-j)-(t/2)) for i,j in zip(a,b)] # calculate the list differences
 b.sort() # sort the list
  a.sort(reverse=True) #sort in reveres
 if verbose: print(a)
 if verbose: print(b)
 m,p=[],[]
  if tlen <=2**9: # if the list is smaller than 2^9, 512 do a thorough comparison
   fast=False
   # find the values closes to the delta and swop to make list sums equal or nearest equal
   for i in range(len(a)):
     for j in range(len(b)):
       v=a[i]-b[j]-int(abs(t/2))
        if verbose: print('{:>2} - {:>2} = {:>3} <-- {} {} '.format(a[i],b[j],v,i,j))</pre>
        m.append(abs(v))
        p.append((i,j))
   i,j=p[m.index(min(m))] #swop the values around
  else: # otherwise if buger than 512 len do a faster compare
   fast=True
   t=(sum(a)-sum(b))
   d=[int((i-j)-(t/2)) for i,j in zip(a,b)]
   e=[abs(i) for i in d]
   #print(min(e),e.index(min(e)))
   i,j=e.index(min(e)),e.index(min(e))
  if verbose: print(m,min(m),m.index(min(m)))
  if verbose: print(p[m.index(min(m))])
  #i,j=p[m.index(min(m))]
  a[i],b[j]=b[j],a[i] # swop the values around
  return a,b,fast
if __name__ == '__main__':
 # generate a range of numbers for increased list lengths for testing
  r=[2**i for i in range(2,21)] # 4 to 1 Million
  for v in r:
   #print(v)
   start=time() # start the time
   l=list(np.random.randint(1,100,v)) # generate a list of values for testing
   a,b=split(l) # split the list of values in tow sublists
   a,b,s = bestdiff(a,b) # return the best solution
   stop=time() # stop the timer
   #display the results
   t=stop-start
   if t < 0.5:
     t*=1000
      st='ms'
    else:
      t*=1
      st='s'
```

```
Last

update:

2020/07/07

11:28

http://hdip-data-analytics.com/programming/dynamic_programmig_questions?rev=1594121283
```

```
print('diff: {2:>3} len: {4:>9,} time: {3:8.3f} {5:>2} fast: {6:}'.format(a,b,sum(a)-
sum(b),t,v,st,s))
diff: 26 len: 4 time: 0.496 ms fast: False
```

diff:	3 len:	8	time:	0.000	ms	fast:	False
diff:	-1 len:	16	time:	0.495	ms	fast:	False
diff:	1 len:	32	time:	0.992	ms	fast:	False
diff:	1 len:	64	time:	3.965	ms	fast:	False
diff:	0 len:	128	time:	13.399	ms	fast:	False
diff:	0 len:	256	time:	32.237	ms	fast:	False
diff:	0 len:	512	time:	4.465	ms	fast:	True
diff:	-1 len:	1,024	time:	8.929	ms	fast:	True
diff:	0 len:	2,048	time:	14.884	ms	fast:	True
diff:	0 len:	4,096	time:	25.296	ms	fast:	True
diff:	0 len:	8,192	time:	57.052	ms	fast:	True
diff:	0 len:	16,384	time:	92.770	ms	fast:	True
diff:	-1 len:	32,768	time:	208.359	ms	fast:	True
diff:	0 len:	65,536	time:	374.552	ms	fast:	True
diff:	-1 len:	131,072	time:	0.964	S	fast:	True
diff:	-1 len:	262,144	time:	1.631	S	fast:	True
diff:	-1 len:	524,288	time:	3.240	S	fast:	True
diff:	-1 len:	1,048,576	time:	5.768	S	fast:	True

Ways to Cover a Distance

Code

```
111
Count number of ways to cover a distance
Given a distance 'dist, count total number of ways to
cover the distance with 1, 2 and 3 steps.
Examples :
Input: n = 3
Output: 4
Below are the four ways
1 step + 1 step + 1 step
1 step + 2 step
2 step + 1 step
3 step
Input: n = 4
Output: 7
1.1.1
import itertools as itr
def uniquePermutations(inv):
  return list(set(itr.permutations(inv,len(inv))))
def calcdist(n=3,steps=(1,2,3), verbose=False):
  p=[]
  if n>10:
   print('n need to be less than 10')
    return -1,p
  for i in range(1,n+1):
    l=list(itr.combinations_with_replacement(steps,i))
```

```
for v in l:
     if sum(v)==n:
       if verbose: print('{}: {}-->{}'.format(i,v,sum(v)))
        p.append(v)
       if len(v)>1:
          u=uniquePermutations(v)
          for q in u:
            if verbose: print(q)
            p.append(q)
  return len(list(set(p))), list(set(p))
if __name__ == '__main__':
 #for i in range(1,10):
 for i in range(11):
   ways,steplist=calcdist(i)
   if i<7:
     print('{}: {:>2} --> {}'.format(i,ways,steplist))
   else:
     print('{}: {:>2} --> '.format(i,ways,steplist))
```

Output

```
0: 0 --> []

1: 1 --> [(1,)]

2: 2 --> [(2,), (1, 1)]

3: 4 --> [(1, 2), (1, 1, 1), (3,), (2, 1)]

4: 7 --> [(1, 2, 1), (1, 3), (3, 1), (2, 1, 1), (1, 1, 1, 1), (1, 1, 2), (2, 2)]

5: 13 --> [(3, 2), (3, 1, 1), (1, 1, 3), (1, 2, 2), (2, 2, 1), (1, 1, 2, 1), (1, 3, 1), (2, 1, 1, 1), (1, 2, 1, 1), (2, 3), (2, 1, 2), (1, 1, 1, 2), (1, 1, 1, 1, 1)]

6: 24 --> [(2, 2, 1, 1), (1, 3, 2), (1, 1, 1, 2, 1), (1, 1, 2, 1, 1), (1, 1, 3, 1), (2, 3, 1), (1, 1, 2, 2), (2, 1, 2, 1), (3, 3), (1, 2, 2, 1), (3, 1, 1, 1), (3, 1, 2), (1, 2, 1, 1, 1), (1, 1, 1, 1), (1, 1, 1, 1), (1, 2, 1, 2), (3, 2, 1), (2, 1, 1, 2), (1, 2, 3), (1, 1, 1, 1, 3), (2, 2, 2), (2, 1, 1, 1)]

7: 44 -->

8: 81 -->

9: 149 -->
```

Longest Path In Matrix

Subset Sum Problem

Optimal Strategy for a Game

0-1 Knapsack Problem

Boolean Parenthesization Problem

Shortest Common Supersequence

Matrix Chain Multiplication

Partition problem

Rod Cutting

Coin change problem

Word Break Problem

Maximal Product when Cutting Rope

Dice Throw Problem

Box Stacking

Egg Dropping Puzzle

References

- https://www.geeksforgeeks.org/top-20-dynamic-programming-interview-questions/
- https://medium.com/@codingfreak/top-10-dynamic-programming-problems-5da486eeb360
- https://blog.usejournal.com/top-50-dynamic-programming-practice-problems-4208fed71aa3

From: http://hdip-data-analytics.com/ - HDip Data Analytics

Permanent link: http://hdip-data-analytics.com/programming/dynamic_programmig_questions?rev=1594121283

Last update: 2020/07/07 11:28